

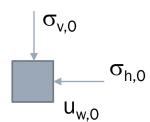
# Geomechanics

LECTURE 12



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Laboratory of soil mechanics - Fall 2024 02.12.2024

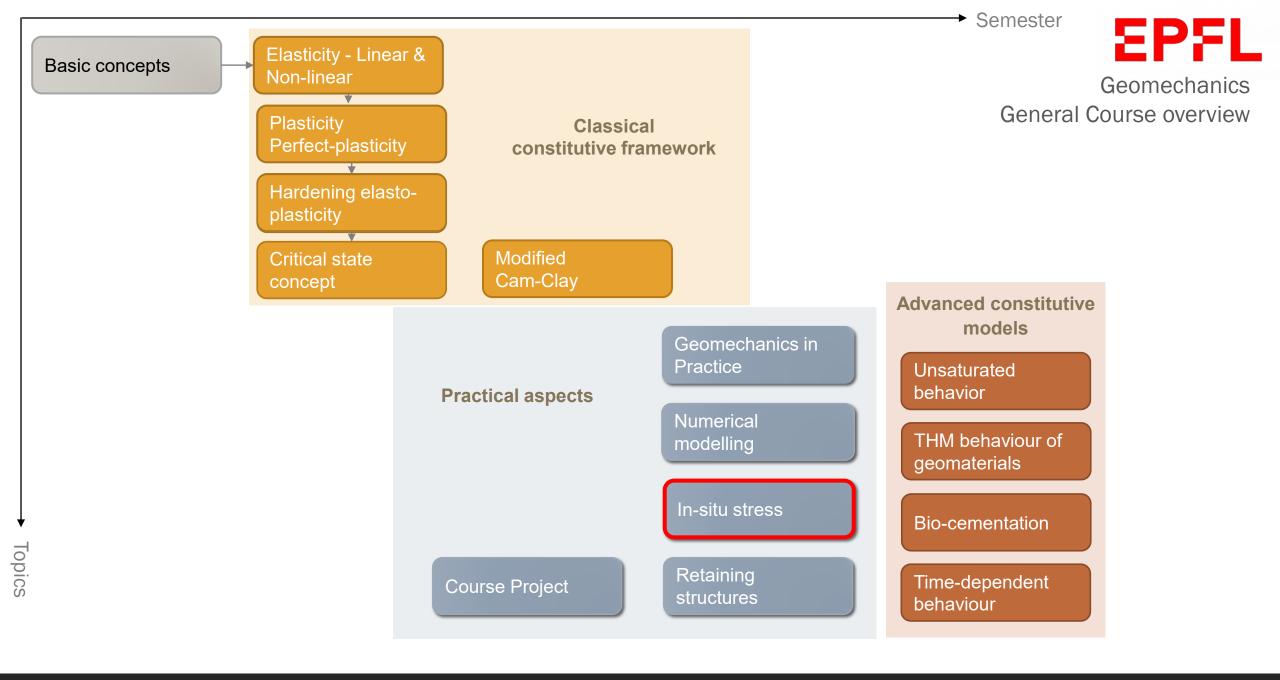




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## Content



- Introduction
- In-situ stress states
- Determination of the in-situ stress



# Introduction

### Some challenging projects

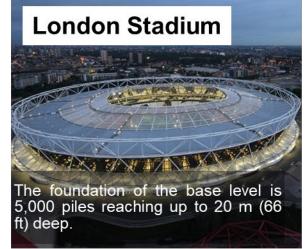


Civil engineering projects may be **onshore** or **offshore** and may involve **different depths** and **different geomaterials.** 









### Geomechanical functional process map



Mission: Solving a complex geomechanical problem for engineering purposes Geomechanics and engineering judgment Strategy: Problem analysis **FORCES** FORCES EXPECTED TO ACT IN THE PRELIMINARY DETAILS + **CURRENTLY** SHORT AND LONG TERM (lifetime of OF THE SITE **ACTING** the structure) **TYPF** GEOMETRY, GEOLOGICAL (mechanical, hydraulic, chemical...; MAGNITUDE INFORMATION... static, dynamic...) Laboratory and **STRESS PATHS** in-situ LABORATORY AND IN-SITU TESTING experimental investigation PARAMETERS FOR DATA DATA **TESTS DESIGN ACQUISITION GEOMECHANICAL MODELLING PROCESSING** Establish the type of The data of interest tests to be carried out, The parameters of interest for the are selected and The data of interest 🛭 the number of tests, and geomechanical model are obtained acquired during the are processed the modalities tests Modelling **GEOMECHANICAL MODEL** approach MODEL NUMERICAL **TYPE OF ANALYSIS CONSTITUTIVE MODEL CREATION** RESOLUTION **PROCESSING** Geometry, **METHOD** AND POST-Mechanical, hydraulic... Elastic materials, loads, AND **PROCESSING** Coupled, decoupled... Elasto-plastic... boundary **SOFTWARE** conditions Design and Strength and displacements Ongoing verification **OBSERVATIONAL METHOD**  $(E_d \leq R_d)$ in-situ activities  $E_d \leq C_d$ project

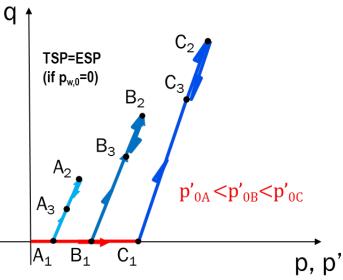
### The importance of knowing the in-situ stress

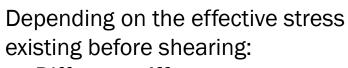


The **initial effective stress** (before any generic stress path takes place) **affects the strength and deformability** of a geomaterial

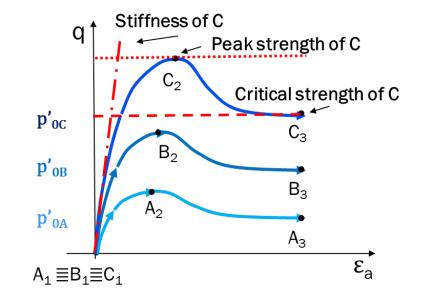
For a given type of stress path, the **mechanical response** will be different depending of the **first point of the stress path**.

EXAMPLE: CTC tests of 3 different specimens (A, B, C): same initial conditions (i.e. same void ratio), consolidated at 3 different initial mean effective stress





- Different stiffness
- Different strength





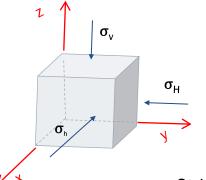
- Prediction of settlements
- Estimation of bearing capacities and lateral earth pressure



### Terminology - Mathematical description



#### A simple and common assumption



$$\boldsymbol{\sigma} = \begin{pmatrix} \boldsymbol{\sigma}_{h} & 0 & 0 \\ 0 & \boldsymbol{\sigma}_{H} & 0 \\ 0 & 0 & \boldsymbol{\sigma}_{v} \end{pmatrix}$$

Strictly valid if horizontal topographic surface in a homogeneous medium, at most according to horizontal layers

State of stress in a point written in the principal stress system assuming the **vertical direction as principal one** 

**4 unknowns:** the **magnitude** of the three principal stresses and the **direction** of one of the two horizontal principal stresses

#### The lateral stress coefficient

#### Coefficient of lateral stress

The **ratio** of one horizontal stress with respect to the vertical effective stress

$$K = \frac{\sigma_i}{\sigma_i}$$

i: generic horizontal stress

#### Coefficient of lateral stress at rest

The ratio of one horizontal stress with respect to the vertical stress in the case of **zero horizontal strains** 

$$\varepsilon_{i} = 0 \rightarrow K_{0} = \frac{\sigma_{i}^{'}}{\sigma_{v}^{'}}$$

i: generic horizontal stress

### Determination of the in-situ vertical stress, $\sigma_v$

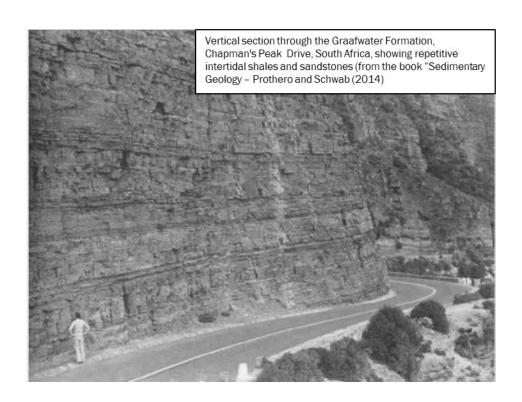


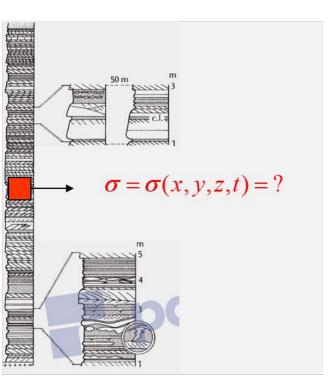
$$\sigma_v = \int_0^z \rho(z) g dz \cong \bar{\rho} g z$$

 $\rho(z)$ : density as a function of depth z

g: gravitational acceleration constant

 $\bar{
ho}$ : mean density of the rocks above the depth z





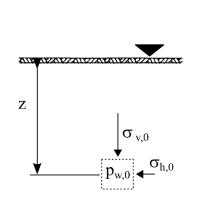
- Average densities are required
- For computing the vertical effective stress it is necessary to know the water pressure at the depth of interest (hydrostatic or not)



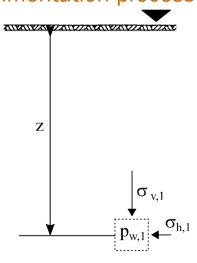
# In-situ stress states



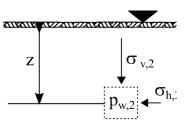
#### Sedimentation process



0)







 $\sigma_v' = \sigma_v - p_w$ 

pressure currently existing

The **vertical effective stress** at each time

depends only on the loads and the water

#### Example:

$$z = 5 m$$
  
 $\gamma_{sat} = 1.9 Mg/m^3$   
 $\gamma' = 0.9 Mg/m^3$   
 $\sigma'_{v} = 44.1 kN/m^2$ 

$$z = 10 m$$
  $z = 3 m$   
 $\gamma_{sat} = 1.9 Mg/m^3$   $\gamma_{sat} = 1.9 Mg/m^3$   
 $\gamma' = 0.9 Mg/m^3$   $\gamma' = 0.9 Mg/m^3$   
 $\sigma'_v = 88.3 kN/m^2$   $\sigma'_v = 26.5 kN/m^3$ 

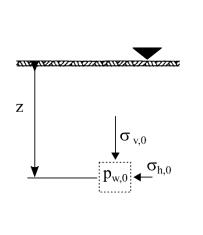
1)

$$z = 3 m$$
  
 $\gamma_{sat} = 1.9 Mg/m^3$   
 $\gamma' = 0.9 Mg/m^3$   
 $\sigma'_v = 26.5 kN/m^2$ 

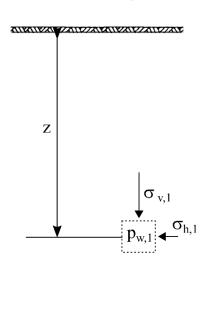
2)

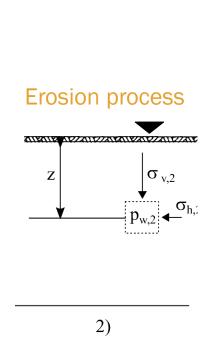


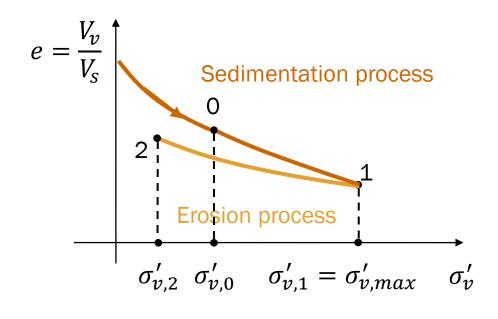
#### Sedimentation process



0)







#### The overconsolidatio ratio (OCR)

$$OCR_{1D} = \frac{\sigma'_{v,max}}{\sigma'_{v,actual}}$$

$$0 \rightarrow 1 \qquad OCR_{1D} = 1$$

1)

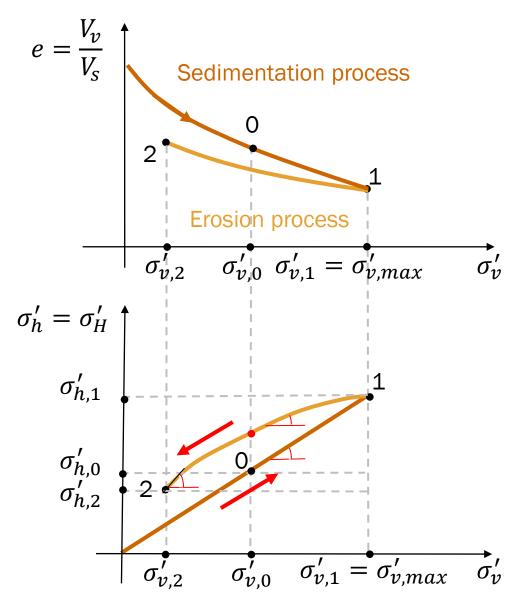
$$1 \rightarrow 2 \quad OCR_{1D} > 1$$

normally consolidated (NC)

overconsolidated (OC)

These types of processes generally involve very large areas, and the horizontal strains are considered negligible.





#### **LOADING - UNLOADING**

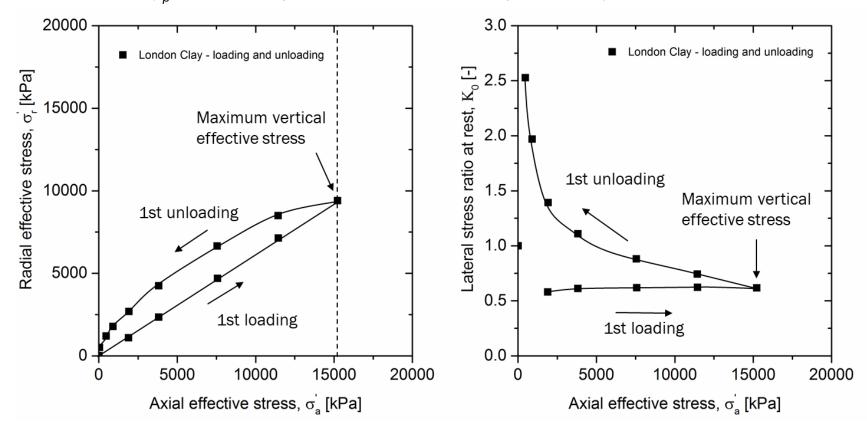
- As the vertical effective stress increases/decreases, the horizontal effective stress increases/decreases
- For a given vertical effective stress, there may be different values of horizontal stress (stress history dependency)
- $K_0$  is constant if the geomaterial is NC
- $K_0$  varies if the geomaterial is OC

Other mechanisms causing overconsolidation are: exacavation, rise of the groundwater table, removal of surcharge loads...



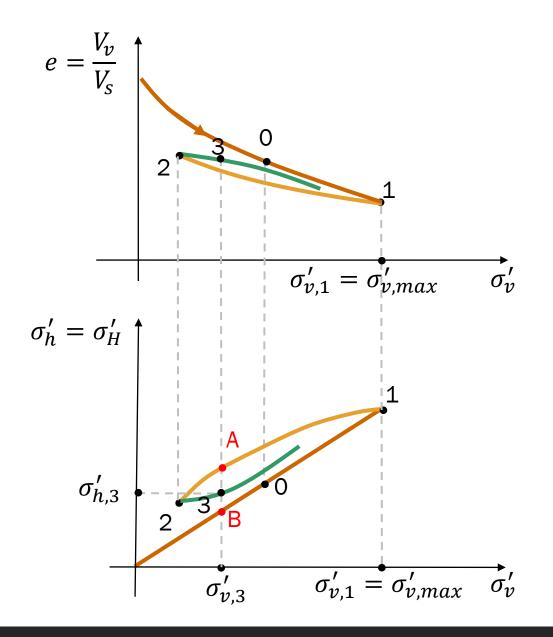
Example of experimental data (Brooker and Ireland, 1965)

LONDON CLAY ( $I_p$ =38.4 %, clay fraction=64 %, c'=1.9, phi'=17.5°) – Oedometer tests



- The trend of the horizontal stress is exactly like the one reported in the previous slide
- During the first loading phase the K<sub>0</sub> remains practically constant
- During the unloading phase (i.e. geomaterial OC)  $K_0$  increases and can reach values much larger than 1.





#### LOADING - UNLOADING - RELOADING

- For a given vertical effective stress, the horizontal effective stress is different depending if we are:
  - in the 1st loading
  - in the 1<sup>st</sup> unloading
  - in the 1st reloading



For a given OCR, there can be a different horizontal effective stress (points A and 3)

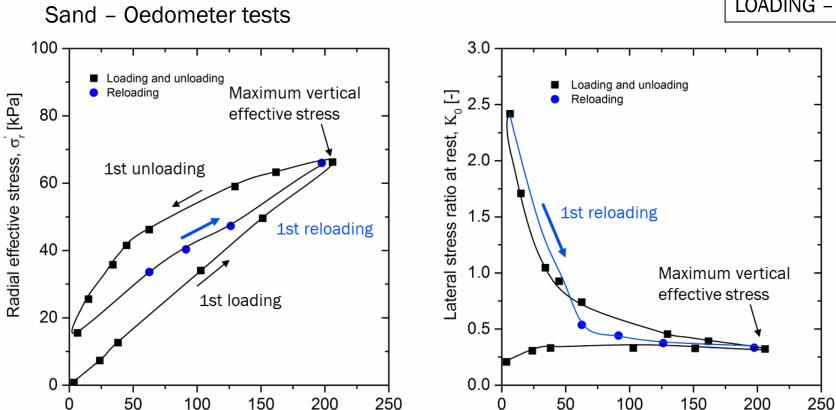
$$OCR_{1D}(A) = \frac{\sigma'_{v,max}}{\sigma'_{v}(A)} \qquad OCR_{1D}(3) = \frac{\sigma'_{v,max}}{\sigma'_{v}(3)}$$
$$OCR_{1D}(A) = OCR_{1D}(3)$$

 Subsequent loading-reloading will follow paths which depends also on the eventual new maximum vertical effective stress reached



Example of experimental data (Mayne and Kulhawy, 1982)

LOADING - UNLOADING - RELOADING



• The trend of the horizontal stress is like the one reported in the previous slide

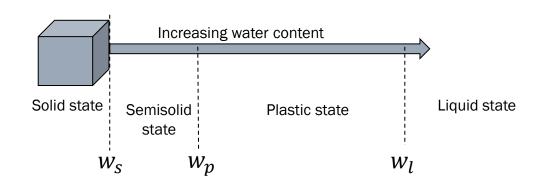
Axial effective stress, σ [kPa]

• During the first reloading phase (i.e. OC geomaterial) the  $K_0$  changes (although to a lesser extent than in the case of  $\mathbf{1}^{\text{st}}$  loading)

Axial effective stress,  $\sigma_a$  [kPa]



Depending on the water content, the same soil can exist under different states (Atterberg's limits)



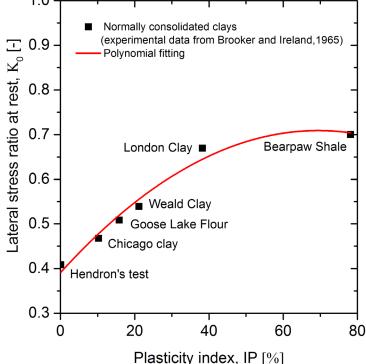
Plasticity index

 $w_l$ : liquid limit

$$I_p = w_l - w_p$$

 $w_p$ : plastic limit





• It affects, among others properties, also the  $K_0$ :

for a NC soil, the higher  $I_p$ , the higher  $K_0$ 

### Key aspects



 In order to completely define the stress state we need all the components of the stress tensor, in the simplest case the problem is reduced to the determination of the vertical effective stress and of the horizontal effective stress.

$$\boldsymbol{\sigma} = \boldsymbol{\sigma}(x, y, z, t) = \begin{pmatrix} \boldsymbol{\sigma}_{xx} & \boldsymbol{\sigma}_{xy} & \boldsymbol{\sigma}_{xz} \\ \boldsymbol{\sigma}_{yx} & \boldsymbol{\sigma}_{yy} & \boldsymbol{\sigma}_{yz} \\ \boldsymbol{\sigma}_{zx} & \boldsymbol{\sigma}_{zy} & \boldsymbol{\sigma}_{zz} \end{pmatrix} \qquad \boldsymbol{\sigma} = \begin{pmatrix} \boldsymbol{\sigma}_{h} & 0 & 0 \\ 0 & \boldsymbol{\sigma}_{H} & 0 \\ 0 & 0 & \boldsymbol{\sigma}_{y} \end{pmatrix}$$

The effective values are computed by knowing the pore water pressure distribution at the site of interest.

• If the geomaterial is of **sedimentary** origin, the horizontal stress can be estimated by knowing the vertical effective stress (no stress history dependency) and the  $K_{0}$ .

$$\sigma_v'$$
 and  $K_0 = \frac{\sigma_h'}{\sigma_v'}$   $\sigma_h' = K_0 \sigma_h'$ 

• The  $K_0$  depends on several factors. For a given geomaterial (e.g. shear strength and plastic characteristics), it is a function of the stress history.



## Determination of the in-situ stress

#### The estimation of the lateral stress coefficient



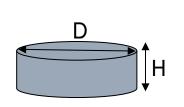
#### How to determine the $K_0$ for your problem? Two different options:

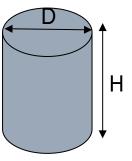
- 1. Perform K<sub>0</sub> tests on your geomaterial(s)
- 2. Use empirical relationship developed thanks to the existing experimental database

#### 1. Perform K0 tests on your geomaterial(s)

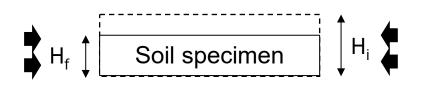
#### Type of laboratory apparatus

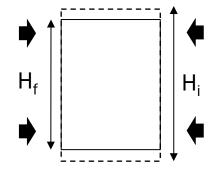
- A special oedometer cell which allows the radial stress measurements or
- A triaxial cell





#### Type of strain

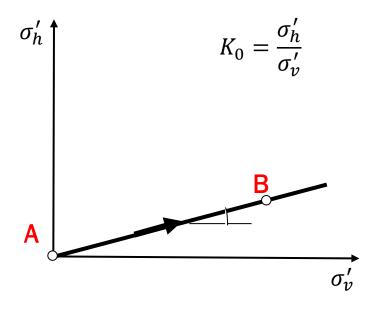


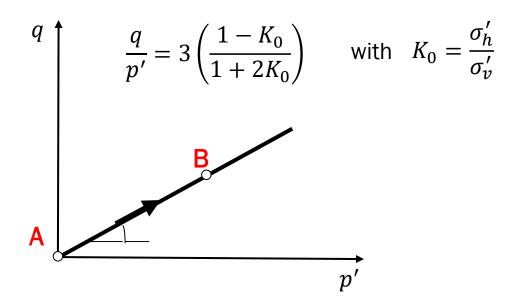


- Axial effective stress is imposed (the actual in-situ vertical effective stress or eventually more complex stress history are reproduced)
- Horizontal strains are prevented
- Radial stress is measured



#### Type of stress path in different planes





The results can be plotted in the plane you prefer (simply you will get different slopes depending on the variables you choose) but in practice you can estimate  $K_0$  for the vertical effective stress of interest (or directly the horizontal stress).

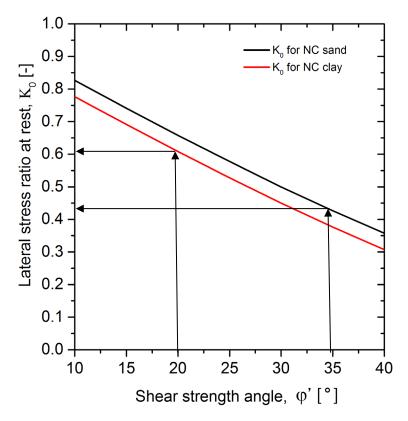
### **Empirical relations**



#### 2. Use empirical relationship developed thanks to the existing experimental database

Several  $K_0$  tests have been performed in the past, therefore different formulas have been provided relating the  $K_0$  to other parameters

NC geomaterials (i.e. they have never been subjected to a higher effective stress than the current one)



$$K_0 \cong 1 - \sin \varphi'$$
 For NC sand (Jaky, 1944)

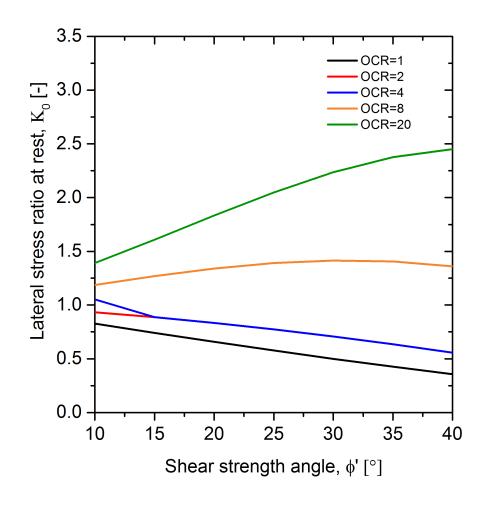
$$K_0 \cong 0.95 - \sin \varphi'$$
 For NC clay (Brooker and Ireland, 1965)

The shear strength angle needs to be known

### Empirical relations



OC geomaterials (i.e. they have been subjected to a higher effective stress than the current one)



For a simple loading unloading process (statistical study on 170 different soils)

$$K_0 = (1 - \sin\varphi')OCR^{\sin\varphi'}$$

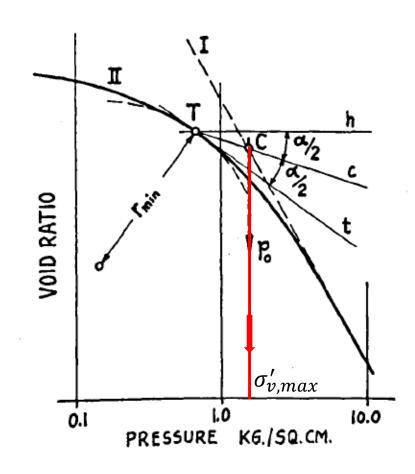
Mayne and Kulhawy (1982)

The shear strength angle and the OCR need to be known

### **Empirical relations**



#### <u>Determination of the OCR – Casagrande's method</u>



$$OCR_{1D} = \frac{\sigma'_{v,max}}{\sigma'_{v,actual}}$$

Oedometer tests

Post processing stages:

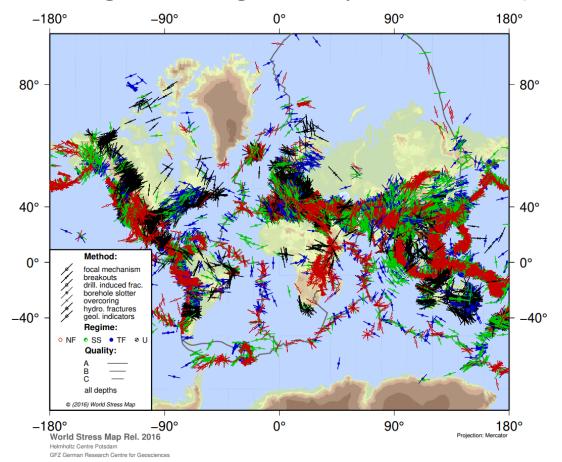
- a. Identification of the maximum point of curvature of the experimental curve in the plane  $e-\sigma'_v$  (i.e. point T).
- b. The horizontal (h) and the tangent (t) to the curve passing through point T are traced.
- c. The bisector of the angle between t and h is determined.
- d. The intersection between the straight line of the experimental curve and the bisector is determined.

Casagrande, 1936. The determination of the pre-consolidation load and its practical significance.

### The World Stress Map (WSP)



- It collects existing information of the stress state of the Earth's crust (42,870 data records within the upper 40 km of the Earth's crust).
- Data are classified according to the method used to estimate them and a quality index is associated with each information.
- It is useful for a global and regional analysis of the stress patterns.



#### **Useful information**

- The orientation of the maximum horizontal stress component.
- The tectonic regime deduced from the stress information.

#### **Example of applications**

Reservoirs, tunnel, boreholes, waste disposal sites

Map generated with CASMO

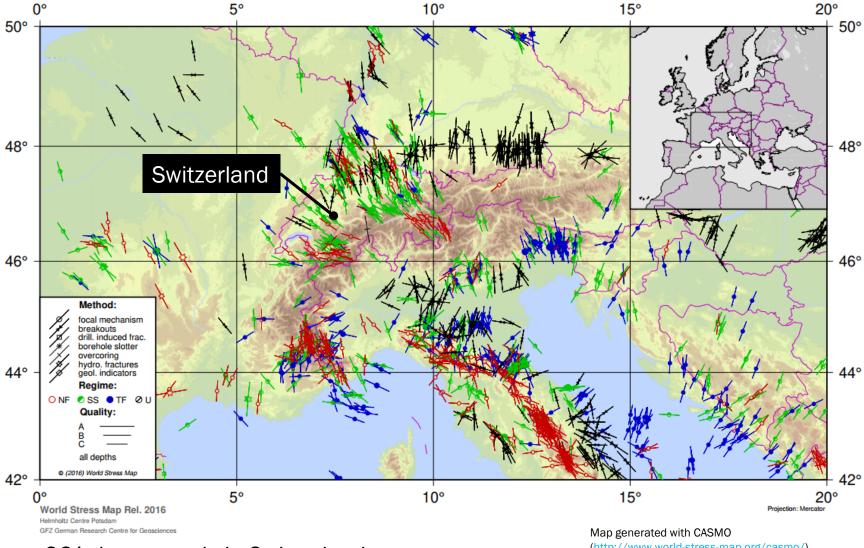
(http://www.world-stress-map.org/casmo/)

Heidbach, Oliver; Rajabi, Mojtaba; Reiter, Karsten; Ziegler, Moritz; WSM Team (2016):

World Stress Map Database Release 2016. V. 1.1. GFZ Data Services. http://doi.org/10.5880/WSM.2016.001

### The World Stress Map (WSP)





261 data records in Switzerland between 0 and 30 km depth

(http://www.world-stress-map.org/casmo/)

Heidbach, Oliver; Rajabi, Mojtaba; Reiter, Karsten; Ziegler, Moritz; WSM Team (2016): World Stress Map Database Release 2016. V. 1.1.

GFZ Data Services. http://doi.org/10.5880/WSM.2016.001

### Key aspects



- Knowing the stress state at one point means knowing the components of a second order tensor.
- 2. The initial stress state is the **first point of a generic stress path**; it affects the **stiffness** and **strength** of the geomaterial.
- 3. Under the common assumption of verticality and horizontality of the principal stresses, only the vertical effective stress and the  $K_0$  must be estimated.
- 4. The coefficient of lateral stress is a function of several factors and depends not only on the loads currently acting but also on the loads that were acting in the past. It is important to know if the geomaterial is normal-consolidated or overconsolidated.
- 5. K<sub>0</sub> can be estimated by asking for K<sub>0</sub>-laboratory tests or by using formulas of empirical derivation.
- 6. There is a **database** available on the website <a href="http://www.world-stress-map.org/casmo">http://www.world-stress-map.org/casmo</a> in which some information concerning the orientation of the principal stresses are collected and available for consultation.



## Thank you for your attention

